Getting started with NumWorks (Statistics)

This year we will be using the NumWorks graphing calculator in our math class! This activity will help you get to know the calculator and some of the features we will be using in this class.

The keyboard

Before we get started, let's take a closer look at the keyboard. You'll see it is arranged into three different zones.

In the bottom section, you will find basic operations and the number pad. Notice that there is only one minus key. Here you will also find the (Ans) key which allows you to use the most recent result in your calculations. To compute a calculation, press the (EXE) key.

In the middle section, you will find some advanced functions and commonly used values. What keys do you recognize in this section?

In the top row of the Advanced Functions section, you will find the (shift) key which gives you access to the yellow option of each key. The (ALPHA/alpha) key can be used select the alpha characters on each key. The (x,n,t) key is a quick way to enter x (or other variables as needed). The (var) key opens a menu of stored values. The **Toolbox** (paste) provides additional functions organized in categories. Finally, the (clear) key works just like on your computer or phone to backspace.

The top section is the Navigation Zone where you have arrow keys to navigate the screen, the (ok) key to make selections and a (↰) key to take you back to a previous menu. The (⌂) button will return you to the home screen and the (⏻) button turns the calculator on and off.

Navigate around the home screen. How many applications are there?

The applications

The NumWorks calculator is app-based, just like a phone. That means you will open different applications based on the task you are completing. Let's dive into some of the apps to see what they do!

Calculation

The **Calculation** application is where you will do all of your... calculations!

Navigate to the Calculation application and open it by pressing OK.

1. Let's add some fractions! By hand, add $\frac{1}{6} + \frac{1}{2}$.

$$\frac{1}{6} + \frac{1}{2}$$
$$= \frac{1}{6} + \frac{3}{6}$$
$$= \frac{4}{6}$$
$$= \frac{2}{3}$$

2. Check your work by using the calculator. What do you notice about your answer?

To input $\frac{1}{6}$, press the $\boxed{1}$ key followed by the $\boxed{\div}$ key. Then press the $\boxed{6}$ key. Use the $\boxed{\triangleright}$ key to get out of the denominator before adding the other fraction.

| rad | CALCULATION | |

$$\frac{1}{6} + \frac{1}{2} \qquad \frac{2}{3} \approx 0.6666666667$$
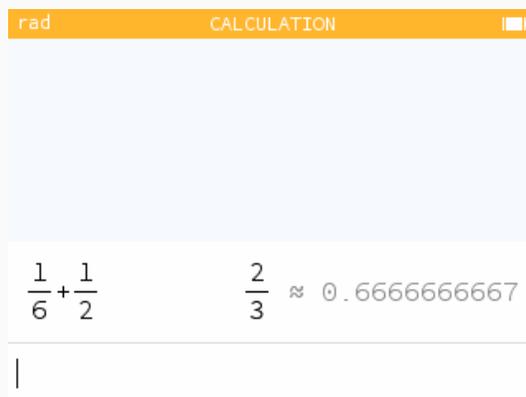
The calculator provides both the simplified fraction and decimal approximation.

3. Use your calculator to subtract $\frac{9}{5} - \frac{4}{10}$.
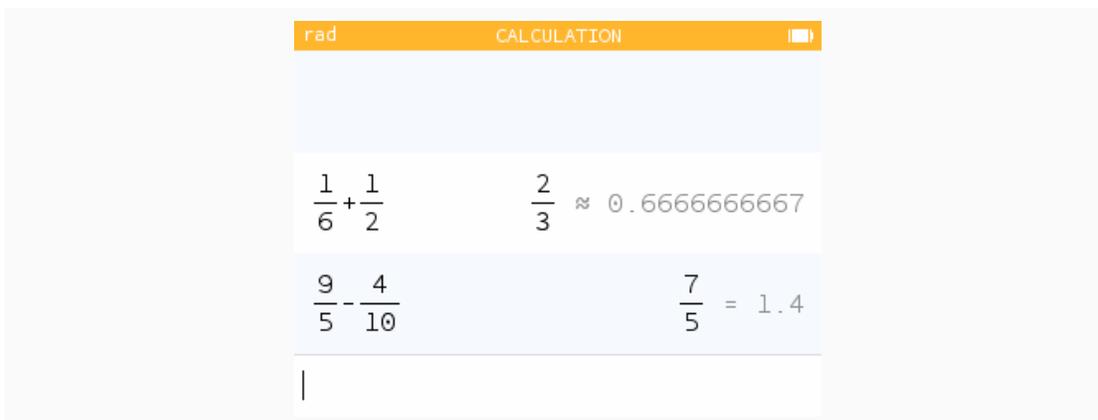
4. How do the results of the last two calculations differ?

For the first calculation, the decimal result was an approximation and the "approximately equal to" symbol was used. In the second calculation, the decimal result was exact and the "equal to" symbol was used.

5. Navigate up into the *calculation history* and click on the three dots on the right side of the screen to view the *additional results*. What additional results are provided for this calculation?

Use the △ key to navigate into your *calculation history*. Navigate over to the three dots and press ⊙.
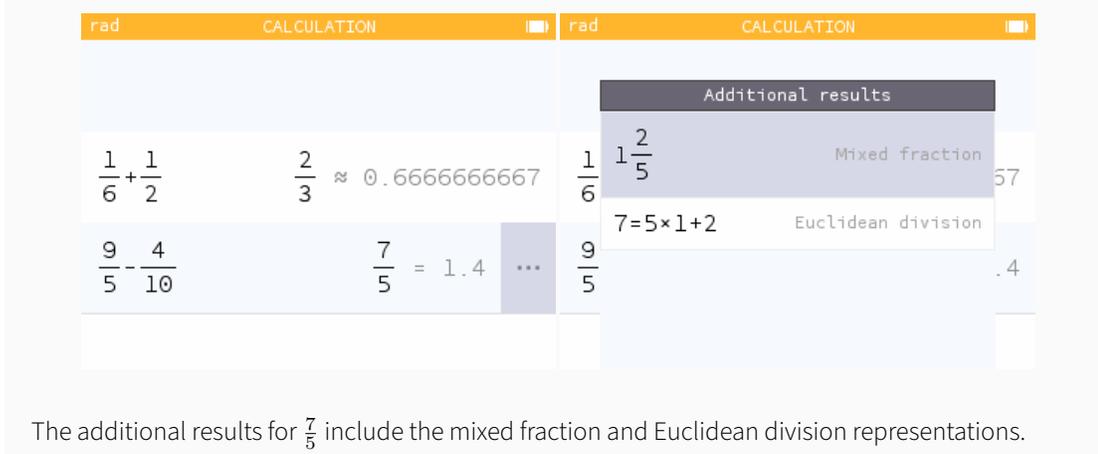
The additional results for $\frac{7}{5}$ include the mixed fraction and Euclidean division representations.

6. Return to the editing bar and open the **Toolbox**. Navigate through the Toolbox and list any functions that you know.
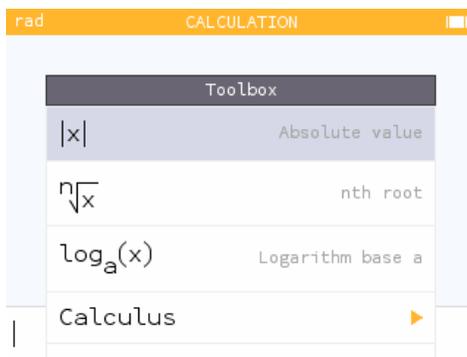
Press the ⟲ key until you return to the editing bar. Open the **Toolbox** by pressing the 📟 key. Student responses will vary.

7. How many ways are there to select four plants out of the six that are available? Within the **Toolbox** 📟, open the **Probability** section and select **Combination**. Input $\binom{6}{4}$.

There are 15 ways to select 4 plants out of 6.

Grapher

Graphing relations and functions is simple within the **Grapher** application.

Our goal will be to graph the linear function $f(x) = 3x + 5$, look at its features and view the table.
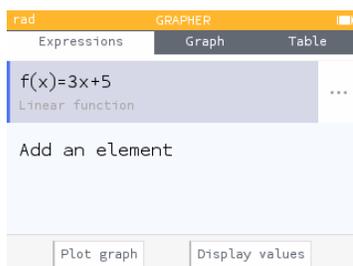
Notice that there are three tabs at the top of the screen: **Expressions**, **Graph** and **Table**.

The **Expressions** tab is where you will enter your function.

1. Press ⓞⓚ to **Add an element**. There are some templates you can use when entering expressions. For this example, select the $f(x) = x$ template.
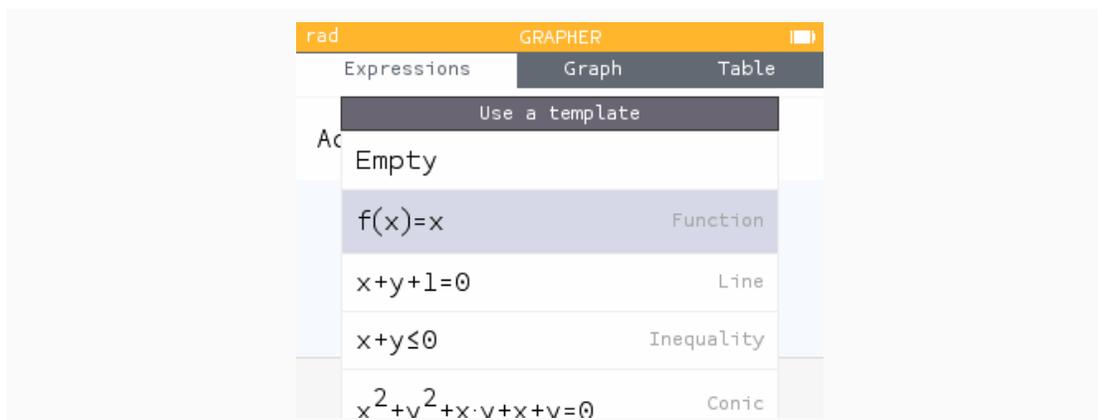

2. Input the function $f(x) = 3x + 5$.

To enter the function $f(x) = 3x + 5$, first use the ◁ key to move your cursor to the left of the x and add the coefficent 3. Now use the ▷ key and finish the expression. Once your function is completed, press ⓞⓚ or ⒺⓍⒺ.

The **Graph** tab will plot the graphs of your functions and provide tools for exploring key characteristics.
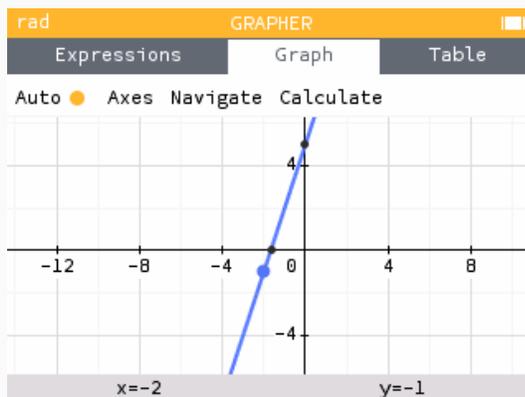
1. View the graph. The **auto** zoom generally provides a window that you will find useful.
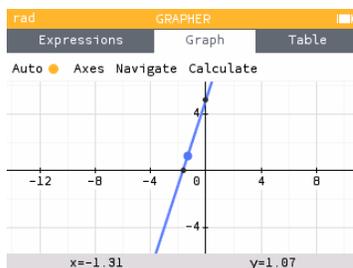
To view the graph, either navigate down to **Plot graph** or up and over to the **Graph** tab and press ⓞⓚ.

2. Press the ⊕ⁿ and ⊝ keys to zoom in and out.

3. Navigate to $x = -2$. What is the value of $f(x)$?

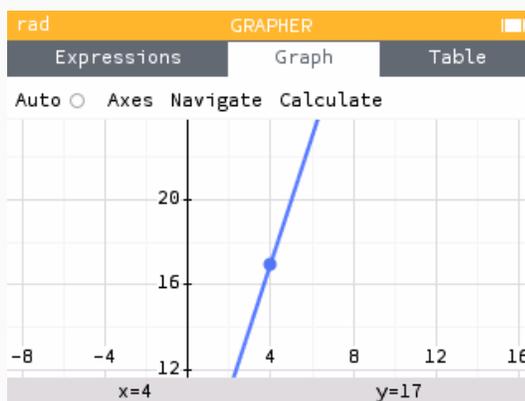Calculations — Graphing — Boxplots — Histograms — Regression   5

Use the ◁ and ▷ keys to trace the line.

When $x = -2$, $f(x) = -1$.

4. What is the value of $f(x)$ when $x = 4$?

Press the (4ˣ) key followed by ⊛ as a shortcut to quickly navigate to $x = 4$.

When $x = 4$, $f(x) = 17$.

5. Open the **Calculate** menu. Then open the **Find** menu. This menu provides tools for finding key characteristics of our graph. Use the **Inverse image** option to determine the value of x when $f(x) = 10$.
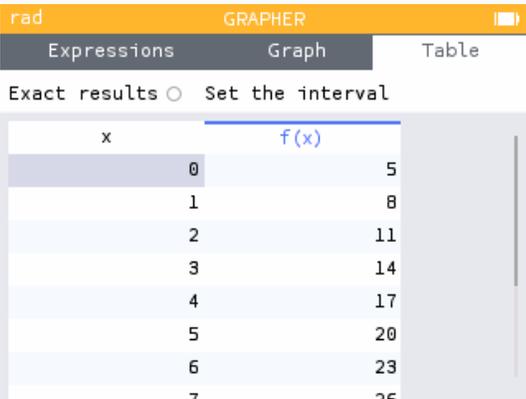
When $y = 10$, $x = 1.667$.

The **Table** tab provides a table of points for your function.

1. Open the **Table** tab.

   To view the table, navigate up and over to the **Table** tab and press ⓞₖ.

rad	GRAPHER	
Expressions	Graph	Table

   Exact results ○ Set the interval

 | x | f(x) |
   |---|---|
   | 0 | 5 |
   | 1 | 8 |
   | 2 | 11 |
   | 3 | 14 |
   | 4 | 17 |
   | 5 | 20 |
   | 6 | 23 |
   | 7 | 26 |

2. The table displays the x and $f(x)$ values for $x = 0$ through $x = 10$. Copy down the values of $f(x)$ in the table below.

x	0	1	2	3	4	5	6	7	8	9	10
f(x)											

x	0	1	2	3	4	5	6	7	8	9	10
f(x)	5	8	11	14	17	20	23	26	29	32	35

3. What is the value of $f(x)$ when $x = 100$?

   Highlight any of the current x-values and type 100. Press ⓔₓₑ. You will now see the value of $f(x)$ in the table.

rad	GRAPHER	
Expressions	Graph	Table

   Exact results ○ Set the interval
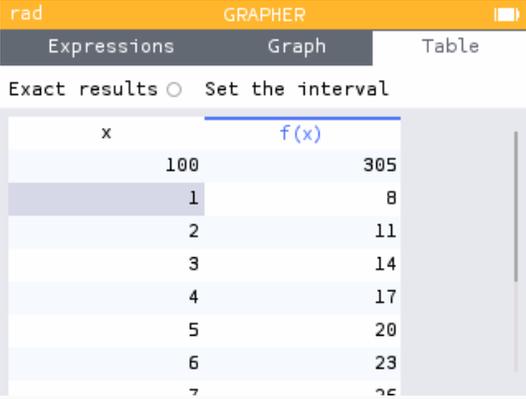
x	f(x)
100	305
1	8
2	11
3	14
4	17
5	20
6	23
7	26

When $x = 100$, $f(x) = 305$.

Statistics

The **Statistics** application is great for studying graphical representations of data sets and viewing summary statistics

Open the Statistics app and notice the three tabs at the top of the screen: **Data**, **Graph** and **Stats**.

The **Data** tab is where you will enter your data.

The table below shows the number of text messages sent in the past 24 hours by the students in a class.

Table 1: Number of texts sent in past 24 hours

0	7	1	29	25	8	5	1	25	98	9	0	26	8	118	72	0	92	52	14	3	3	44	5	42

1. On the **Data** tab, enter the values into the **V1** column. What do you think **N1** represents?
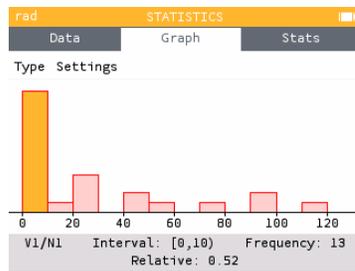

   N1 represents the frequencies. It will default to 1.

2. Once your data is entered, navigate back up to the top of the column and press ⊛ to open the V1 column options. Sort your data.
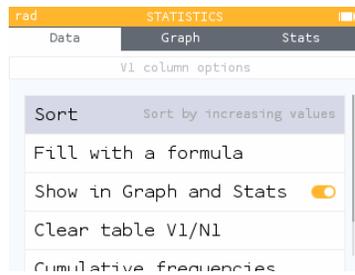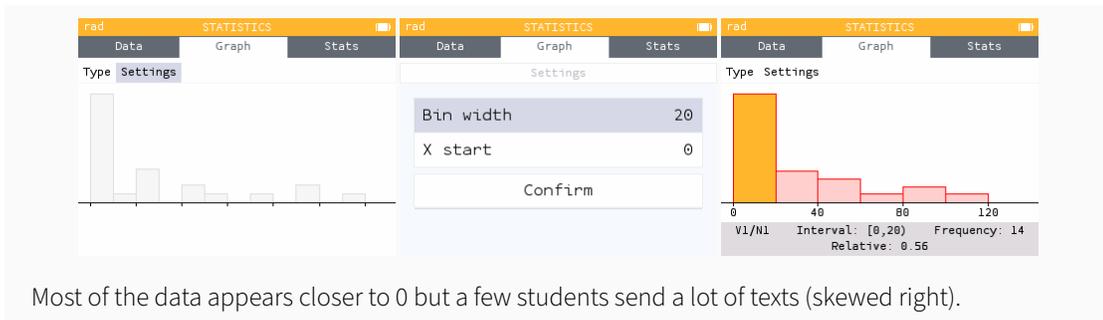
To view graphical representations of your data, you will use the **Graph** tab.

1. Open the **Graph** tab and create a histogram for this data.

2. Navigate through the histogram.

3. The histogram is showing "bins" of size 10. Change the **Bin width** to 20 using the histogram **Settings**. What do you notice about the distribution?

   Most of the data appears closer to 0 but a few students send a lot of texts (skewed right).

4. You can also view a boxplot of the data on number of texts sent. Change the graph from a histogram to a boxplot using the **Type** menu.
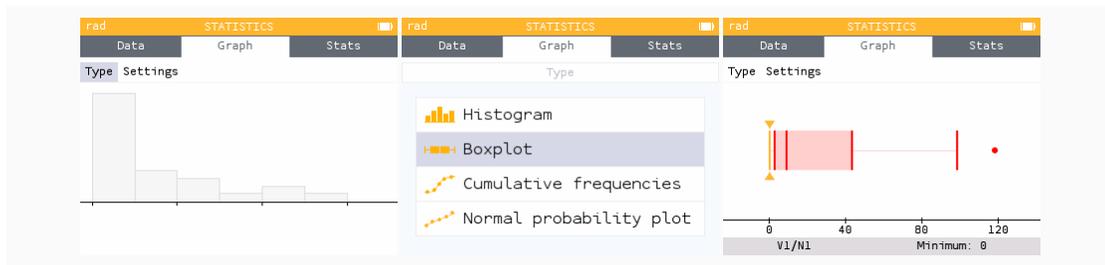
5. Navigate through the boxplot. Record the values shown in the bottom banner.

The bottom banner provides the 5-number summary:

Minimum	First quartile	Median	Third quartile	Upper whisker	Maximum
0	3	9	43	98	118

6. The last value in the boxplot is displayed as a single dot. What does this represent about that data point?

This data point is an outlier.

The **Stats** tab provides summary statistics for the dataset.

1. Open the **Stats** tab. What do you notice about the first few entries on this tab?

The first few values match the values found in the bottom banner of the boxplot.

2. Scroll through the list of summary statistics found on the **Stats** tab. Which of the terms or symbols do you recognize?

Student answers will vary. Make note of the difference between statistics for a population (mean, standard deviation, variance) and those for a sample (sample mean, sample standard deviation, sample variance).

Regression

The **Regression** application plots scatterplots and provides the line of best fit.

Open the Regression application. The Regression app also has three tabs at the top of the screen: **Data**, **Graph** and **Stats**.
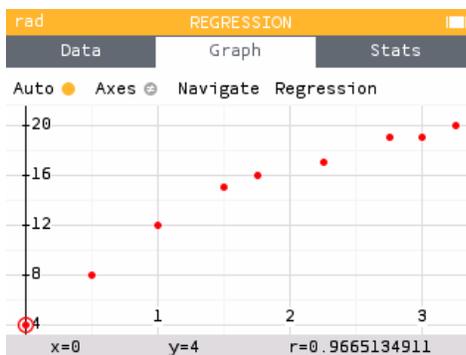
The table below shows the relationship between quiz scores (out of 20) and study time (in hours) for a few students in a class.

Study time (hours)	1.5	3	2.25	1.75	0.5	3.25	1	0	2.75
Score (out of 20)	15	19	17	16	8	20	12	4	19

1. On the **Data** tab, enter the values of "Study time" into the **X1** column and the values of "Score" into the **Y1** column.
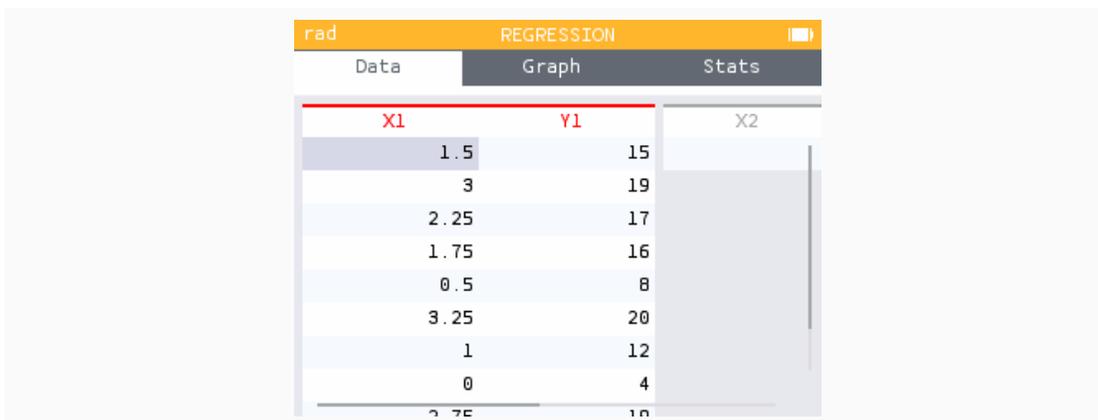
2. Select the **Graph** tab to view the scatterplot.

3. Navigate through the data points. Notice that the values of x and y appear in the bottom banner.

4. How would you describe the relationship between Study time and Score?

> There appears to be a positive, linear relationship. The more time a student studies, the higher their quiz score is.
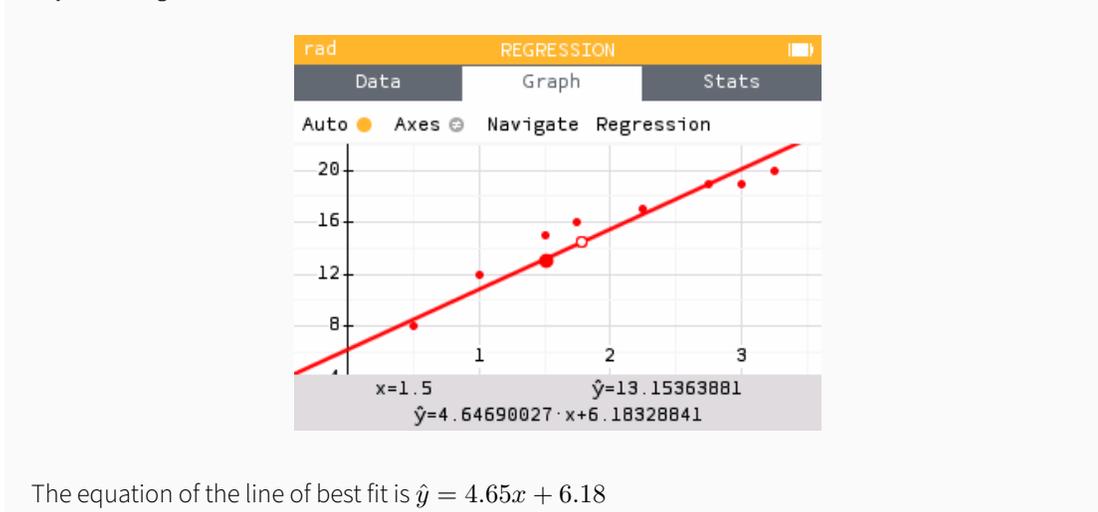
Let's find the line of best fit.

1. While viewing the scatterplot on the **Graph** tab, press (ok) to open the list of regression models.

2. Press (ok) on **Linear**.
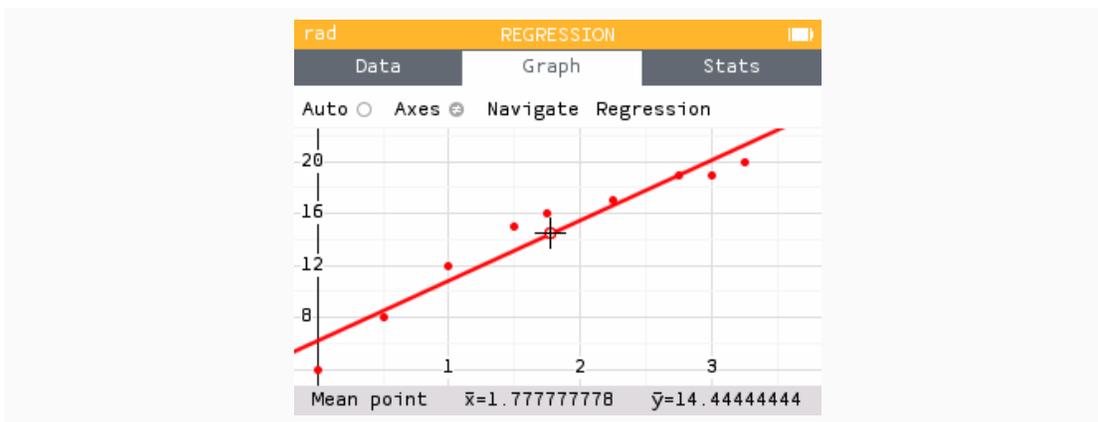
3. Navigate through the data points and onto the line of best fit. What is the regression equation (round to the nearest hundredth)?

> Use the (◀) and (▶) keys to navigate through the data points. While on a data point, use the (△) or (▽) keys to navigate onto the line of best fit.

The equation of the line of best fit is $\hat{y} = 4.65x + 6.18$

4. Find the equation of the line of best fit in the **Regression** menu.

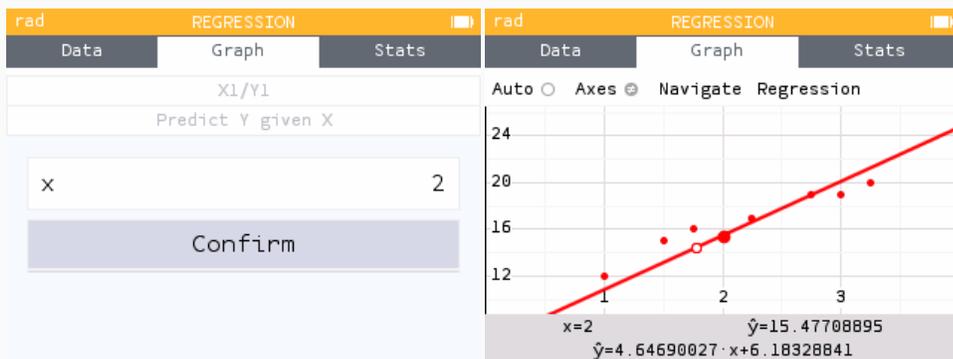Press the (paste) key to open the Regression menu and find the equation of the line.
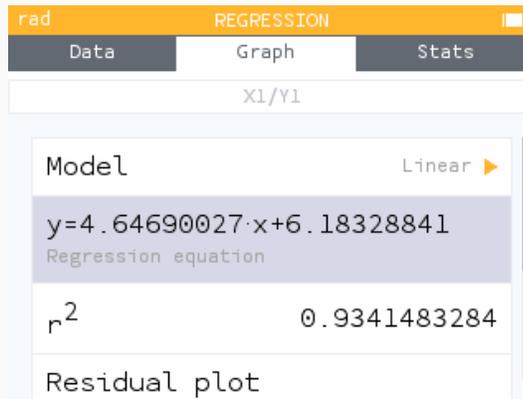
We can use the equation of the line to make predictions for scores based on other study times.

1. While in the **Regression** menu, select **Predict Y given X**.

2. Predict the quiz score for a student who studied for 2 hours.

Enter 2 for x.

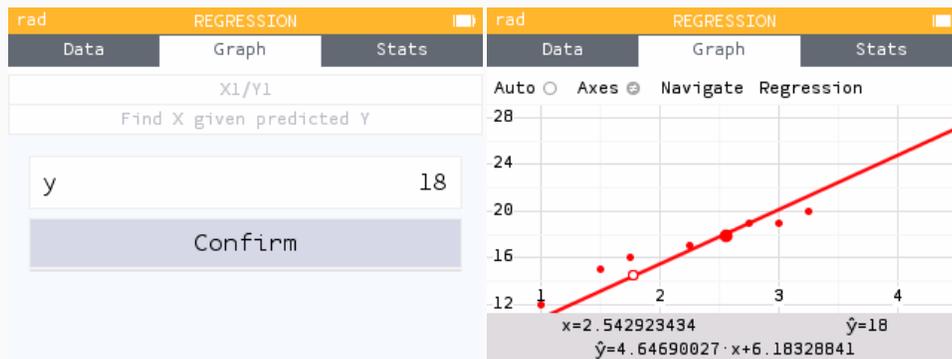A student who studies for 2 hours is predicted to score a 15.48 on average.

3. Return to the Regression menu and select **Find X given predicted Y**.

Use the ↰ key to return the the Regression menu.

rad	REGRESSION	
Data	Graph	Stats

X1/Y1

r^2 0.9341483284

Residual plot

Predict Y given X ▶

Find X given predicted Y ▶
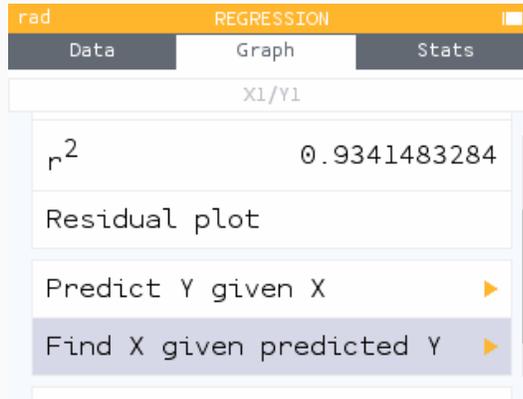
4. Determine how many hours of studying a student would need in order to earn a score of 18 on the quiz.

Enter 18 for y.

rad	REGRESSION			rad	REGRESSION	
Data	Graph	Stats		Data	Graph	Stats

X1/Y1   Auto ○ Axes ⊘ Navigate Regression
Find X given predicted Y

y   18

Confirm

x=2.542923434   ŷ=18
ŷ=4.64690027·x+6.18328841

It is predicted that to earn an 18, a student must study for 2.54 hours, on average.

The **Stats** tab provides summary statistics for our dataset.

1. Navigate to the **Stats** tab and find the row **Mean** $\bar{x}$. This reports the mean or average for X1 and Y1.

rad	REGRESSION	
Data	Graph	Stats

		X1
Mean	$\bar{x}$	1.777778
Sum	Σx	16
Sum of squares	$\Sigma x2$	38.75
Standard deviation	σ	1.070076
Variance	$\sigma 2$	1.145062
Sample std deviation	s	1.134987
Number of points	N	
Covariance	cov	

2. What is the average amount of time these students studied (round to the nearest hundredth)?

rad	REGRESSION	
Data	Graph	Stats
	X1	Y1
Mean $\bar{x}$	1.777778	14.44444
Sum $\sum x$	16	130
of squares $\sum x2$	38.75	2116
deviation σ	1.070076	5.144816
Variance $\sigma 2$	1.145062	26.46914
deviation s	1.134987	5.456902
of points N		9
Covariance cov		5.320988

The average amount of time studied by these students is 1.78 hours.

3. What is the average quiz score for these students (round to the nearest hundredth)?

rad	REGRESSION	
Data	Graph	Stats
	X1	Y1
Mean $\bar{x}$	1.777778	14.44444
Sum $\sum x$	16	130
of squares $\sum x2$	38.75	2116
deviation σ	1.070076	5.144816
Variance $\sigma 2$	1.145062	26.46914
deviation s	1.134987	5.456902
of points N		9
Covariance cov		5.320988

The average score made by these students is 14.44

Keep exploring!

There's a lot more you can do on the NumWorks calculator! Keep exploring the applications and check out the short tutorials at num.works/tutorials.